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Roll No. 2019

S. No. of Question Paper: 8597

Unique Paper Code : 32351101

Name of the Paper : Calculus

Name of the Course : B.Sc. (Hons.) Mathematics

Semester : I

Duration: 3 Hours Maximum Marks: 75

(Write your Roll No. on the top immediately on receipt of this question paper.)

All sections are compulsory.

All questions carry equal marks.

Use of non-programmable scientific calculator is allowed.

Section I

Attempt any four questions from Section I.

1. State Leibnitz's theorem for finding *n*th derivative of product of two functions. If $y = a \cos(\ln x) + b \sin(\ln x)$, prove that $x^2y_{n+2} + (2n+1)xy_{n+1} + (n^2+1)y_n = 0$.

Evaluate the following limit :



$$\lim_{x \to 0^+} x^{\sin x}$$

- 3. Find the intervals of increase and decrease of the following function, discuss its concavity and then sketch its graph $y = (x+1)^2(x-5)$.
- 4. Sketch the graph of the polar curve $r = 3\cos 2\theta$.
- 5. A manufacturer estimates that when 'x' units of a particular commodity are produced each month, the total cost (in dollars) will be $C(x) = \frac{1}{8}x^2 + 4x + 200$ and units can be sold at a price of p(x) = 49 x dollars per unit. Determine the price that corresponds to the maximum profit.

Section II

Attempt any four questions from Section II.

- 6. Find a reduction formula for $\int \csc^n x \, dx$, $n \ge 2$ is an integer. Evaluate $\int \csc^4 x \, dx$.
- 7. Find the volume of the solid generated when the region bounded by $y = \sqrt{25 x^2}$, y = 3, is revolved about the x-axis.

- 8. The base of a certain solid is enclosed by $y = \sqrt{x}$, y = 0, and \Leftrightarrow learndu.in
 - x = 4. Every cross-section perpendicular to the x-axis is a semicircle with its diameter across the base. Find the volume of the solid.
- 9. Find the arc length of the parametric curve:

$$x = (1 + t)^2$$
, $y = (1 + t)^3$, $0 \le t \le 1$.

10. Find the area of the surface generated by revolving the curve $y = \sqrt{4 - x^2}$, $-1 \le x \le 1$, about the x-axis.

Section III

Attempt any three questions from Section III.

- 11. Find the equation of the parabola whose focus is (-1, 4) and directrix is x = 5.
- 12. Find the equation of the hyperbola whose foci are (1, 8) and (1, -12) and vertices are 4 units apart.
- 13. Describe the graph of the equation :

$$9x^2 + 4y^2 + 18x - 24y + 9 = 0.$$



14. Identify and sketch the curve :



$$x^2 + 4xy - 2y^2 - 6 = 0$$
.

Section IV

Attempt any four questions from Section IV.

15. Evaluate:

$$\lim_{t\to 0^+} \left[\frac{\sin 3t}{\sin 2t}\hat{i} + \frac{\log(\sin t)}{\log(\tan t)}\hat{j} + (t\log t)\hat{k}\right].$$

- 16. The acceleration of a moving particle is $\vec{A}(t) = 24t^2\hat{i} + 4\hat{j}$. Find the particle's position as a function of t if $\vec{R}(0) = \hat{i} + 2\hat{j}$ and $\vec{v}(0) = 0$.
- 17. If a shot putter throws a shot from a height of 5 ft with an angle of 46° and initial speed of 25 ft/sec, what is the horizontal distance of the throw?
- 18. Find $\vec{T}(t)$, $\vec{N}(t)$ and $\vec{B}(t)$ for $\vec{r}(t) = \cos t \hat{i} + \sin t \hat{j} + \hat{k}$ at $t = \frac{\pi}{4}$.
- 19. Show that the curvature of the polar curve $r = e^{\alpha \theta}$ is inversely proportional to r.

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